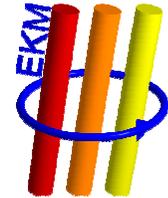




Center for Electronic Correlations and Magnetism  
University of Augsburg



# Surprising effects of the interaction between electrons in solids

Dieter Vollhardt

Symposium “Topical aspects of condensed matter physics”  
on the occasion of Gernot Güntherodt’s 70<sup>th</sup> birthday  
RWTH Aachen, May 3, 2013

Supported by **DFG**

TRR 80



FOR 1346



ALMA MATER  
AQUENSIS

1987/1988



Professor Dr. sc. nat. Gernot **Güntherodt**

Geboren am 27. April 1943 in Themar, Thüringen. – 1963 Abitur. – 1963–68 Studium der Physik an der ETH Zürich. – 1968–73 Wissenschaftlicher Assistent am Laboratorium für Festkörperphysik der ETH Zürich. – 1973 Promotion. – 1974–75 Postdoctoral Fellow am IBM T. J. Watson Research Center, Yorktown Heights, USA. – 1975–80 Permanenter Wissenschaftlicher Mitarbeiter am Max-Planck-Institut für Festkörperforschung in Stuttgart. – 1979 Ernennung zum C3-Professor am II. Physikalischen Institut der Universität zu Köln. – Seit 1980 Teilprojektleiter im Sonderforschungsbereich 125 (Aachen–Jülich–Köln). – 1981, 1982, 1986 Forschungsaufenthalte in USA (IBM, AT + T Bell Labs.) – 1983–85 Member of the Editorial and Executive Board of „European Journal of Physics“. – April 1987 Ernennung zum C4-Professor und Institutsdirektor am 2. Physikalischen Institut (Lehrstuhl II A) der RWTH Aachen.



Professor Dr. rer. nat. Dieter **Vollhardt**

Geboren am 8. September 1951 in Bad Godesberg. – 1969–71 United World College of the Atlantic, S.-Wales, UK. – 1971 Britischer, amerikanischer, deutscher und internationaler Schulabschluß. – 1971–76 Studium der Physik in Hamburg. – 1976–77 Forschungsaufenthalt an der University of Southern California (USC), Los Angeles, USA. – 1977 Physik-Diplom. – 1978–79 Doktorarbeit an der USC, Los Angeles, USA. – 1979 Promotion zum Dr. rer. nat. an der Universität Hamburg. – 1979–84 Wissenschaftlicher Angestellter am MPI für Physik und Astrophysik, München. – 1983 Forschungsaufenthalt bei den Bell Laboratories, Murray Hill, USA, und dem Institute for Theoretical Physics, Santa Barbara, USA. – 1984–87 Heisenberg-Stipendiat der DFG. – Seit 10. 1987 Inhaber des Lehrstuhls C für Theoretische Physik und Direktor am Institut für Theoretische Physik.



German-Japanese Symposium, Schloss Ringberg (1990)



International Symposium on Competing Physics  
in Novel Condensed Matter Systems, Würzburg (1994)



German-Japanese Symposium, Sapporo (2000)



Centro Atomico, Bariloche (2008): Men at work



Bariloche (2008): Men at play

# Surprising effects of the interaction between electrons in solids

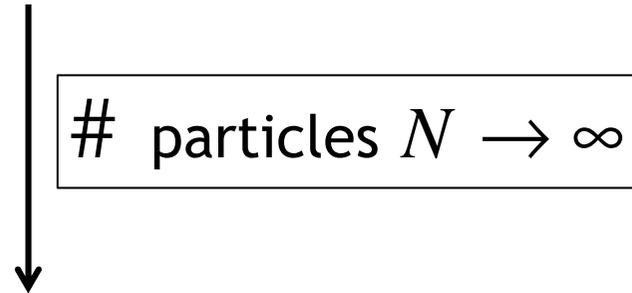
## Outline:

- 1<sup>st</sup> Surprise: Emergence in quantum many-particle systems
- 2<sup>nd</sup> Surprise: Dirt with universal properties
- 3<sup>rd</sup> Surprise: Influence of electronic correlations on the lattice stability of Fe

# 1. Peculiarities of Interacting Many-Particle Systems

# Interacting many-particle systems

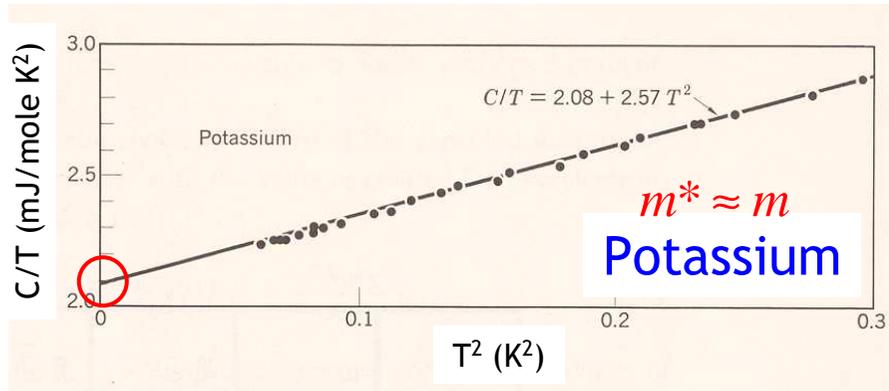
Elementary (“bare”) particles + fundamental interactions



Elementary excitations  
= new particles  
 (“quasiparticles”)

+ effective interactions

# Simple metals

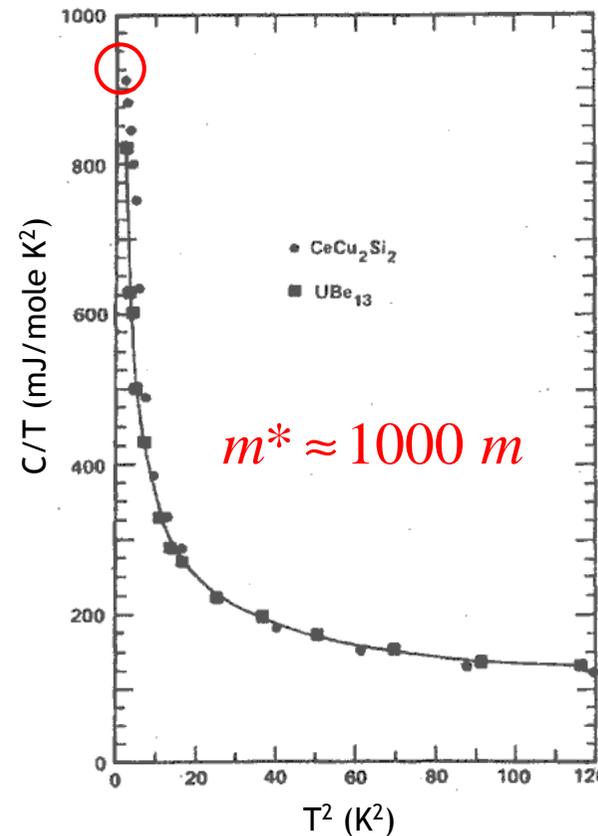


$$\lim_{T \rightarrow 0} \frac{c_V}{T} = \gamma \propto \frac{m^*}{m}$$

Result of elementary excitations (quasiparticles)

# "Heavy Fermions"

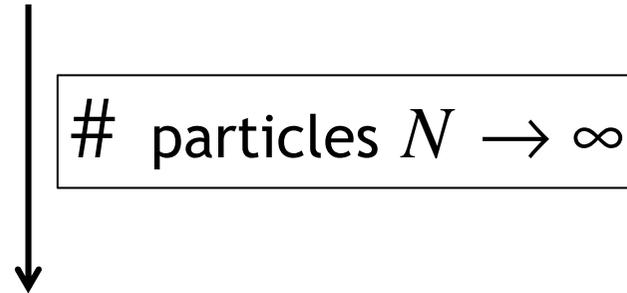
Steglich *et al.* (1979)



CeCu<sub>2</sub>Si<sub>2</sub>, UBe<sub>13</sub>:  
very heavy quasiparticles

# Interacting many-particle systems

Elementary (“bare”) particles + fundamental interactions

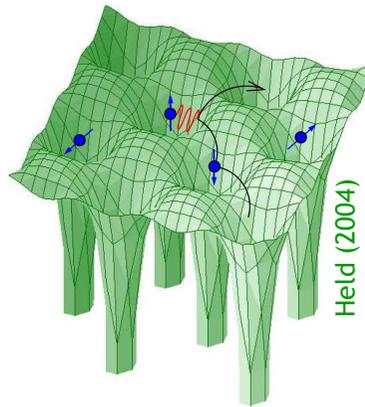


Elementary excitations  
= new particles  
 (“quasiparticles”)

+

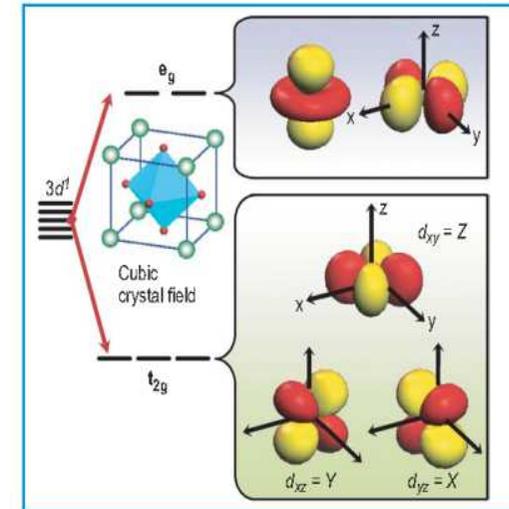
effective interactions

## Electrons in real solids



Complicated modification of  
the bare Coulomb interaction

$Q \bullet \leftarrow r \rightarrow \bullet e$



**Strong effective interaction**  
of electrons in narrow orbitals

# Interacting many-particle systems

↓ # particles  $N \rightarrow \infty$

Entirely new phenomena, e.g., **phase transitions**



Unpredicted behavior **“emerges”**

## Examples:

Superconductivity

Magnetism

Metal-insulator transition

Traffic

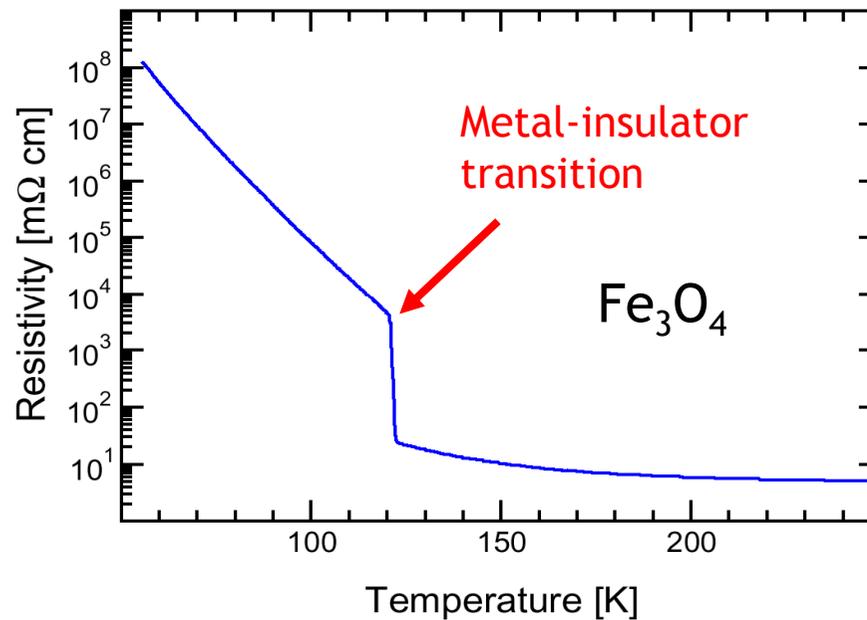
Weather

Stock market

# Interacting many-particle systems

↓ # particles  $N \rightarrow \infty$

Entirely new phenomena, e.g., **phase transitions**



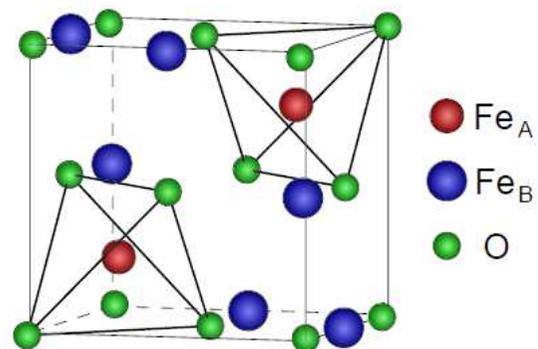
Why?

Example: **Magnetite** ( $\text{Fe}_3\text{O}_4$ )

Macroscopic view



Microscopic view



Electrons in Fe  
are correlated

→ quantum many-particle problem

## 2. Universality of Dirt

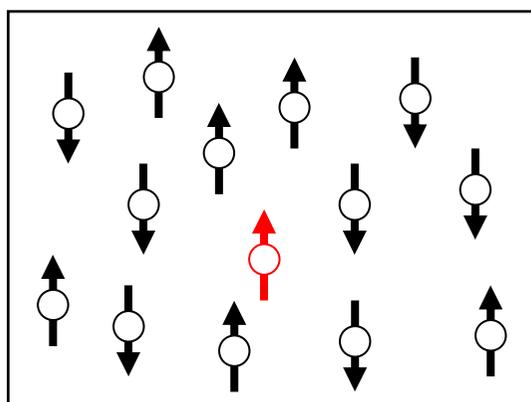


$\text{Fe}_3\text{O}_4$

- “Die Festkörperphysik ist eine Schmutzphysik” (Pauli)
- “One shouldn’t wallow in dirt” (Pauli to Peierls)

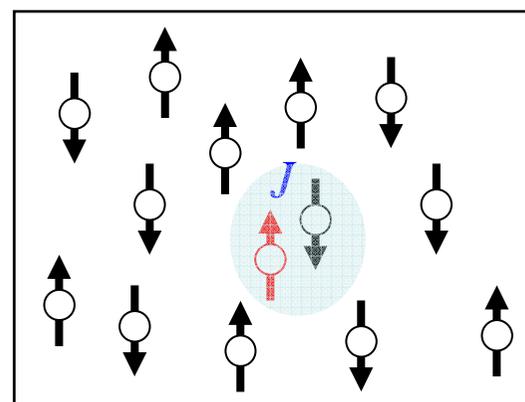
... but “dirt physics” can be fundamental and universal

**Magnetic impurity** in a host of non-interacting (itinerant) electrons



$T > T_K$  (high energies)

Asymptotically free local moment



$T < T_K$  (low energies)

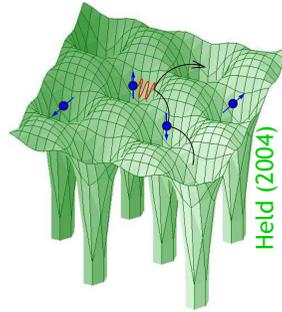
Screening of moment (confinement)

“Kondo effect”

$$T_K \sim E_F e^{-1/|J(\Lambda)|N(E_F)}$$

Prototypical correlation problem with “running coupling constant”  $J(\Lambda)$   
→ QED, QCD

# Theory of Correlated Electron Materials



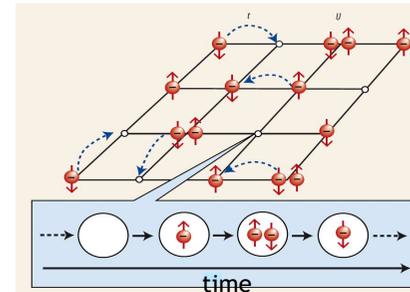
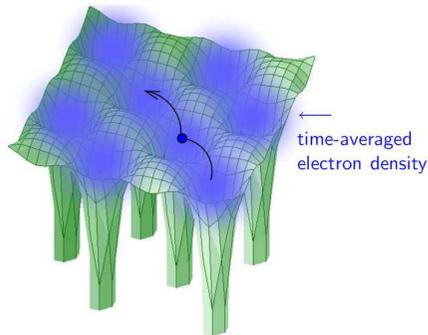
## Comprehensive, non-perturbative approximation scheme needed

DFT/LDA

Model Hamiltonians

- + material specific: "ab initio"
- fails for strong correlations

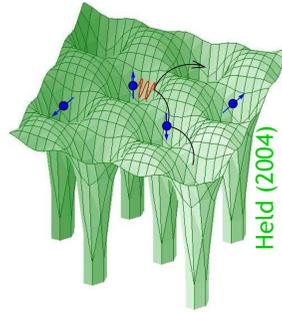
- input parameters unknown: unrealistic
- + systematic many-body approach



**Materials-specific**  
Density functional theory  
(LDA/GGA) or GW



**Correlations-specific**  
Many-body theory



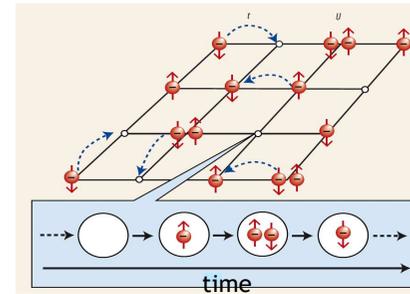
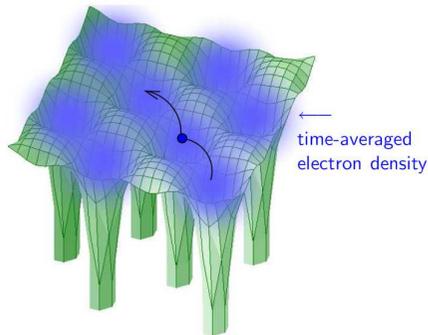
## Comprehensive, non-perturbative approximation scheme needed

DFT/LDA

Model Hamiltonians

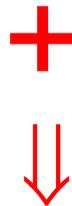
- + material specific: “ab initio”
- fails for strong correlations

- input parameters unknown: unrealistic
- + systematic many-body approach

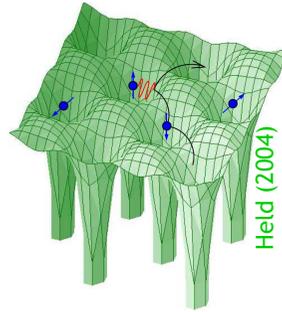


**Materials-specific**  
Density functional theory  
(LDA/GGA) or GW

**Correlations-specific**  
Many-body theory  
(DMFT)

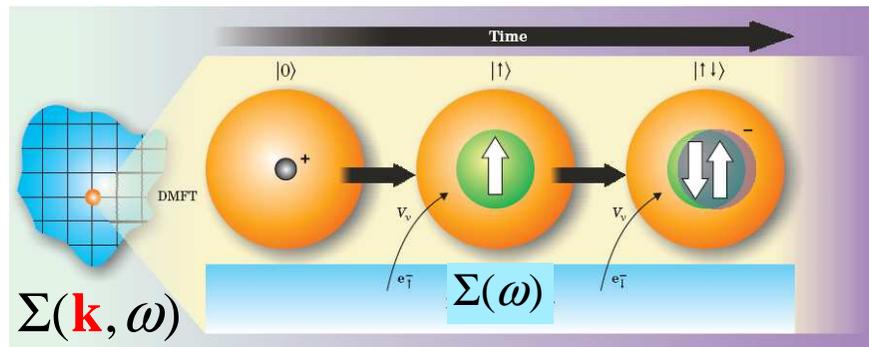


**LDA+DMFT**



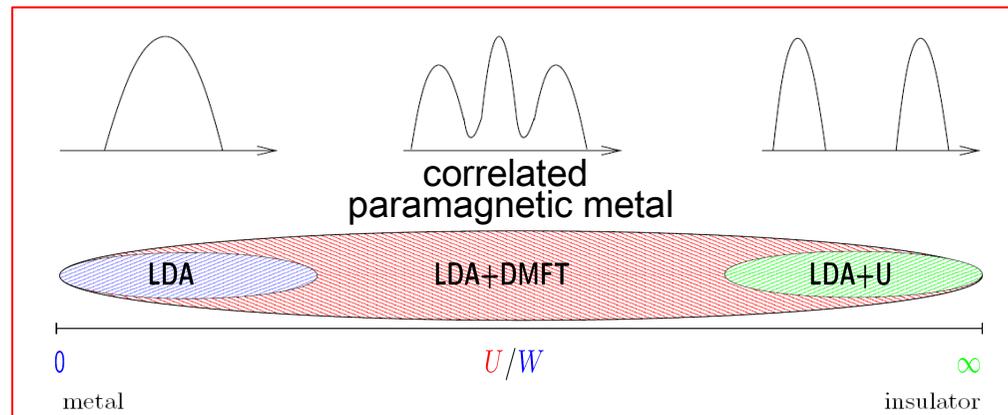
Comprehensive, non-perturbative approximation scheme needed

DMFT



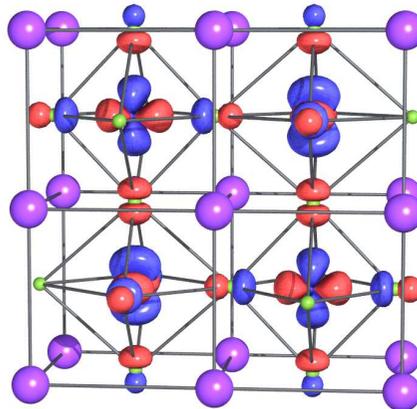
Self-consistent Anderson impurity problem

LDA+DMFT



Until recently: Investigation of electronic correlation effects  
for a **given lattice structure**

→ Influence of electrons on lattice structure ignored



- How do electrons + ions influence **each other** ?
- Can electronic correlations **(de)stabilize** the lattice structure ?

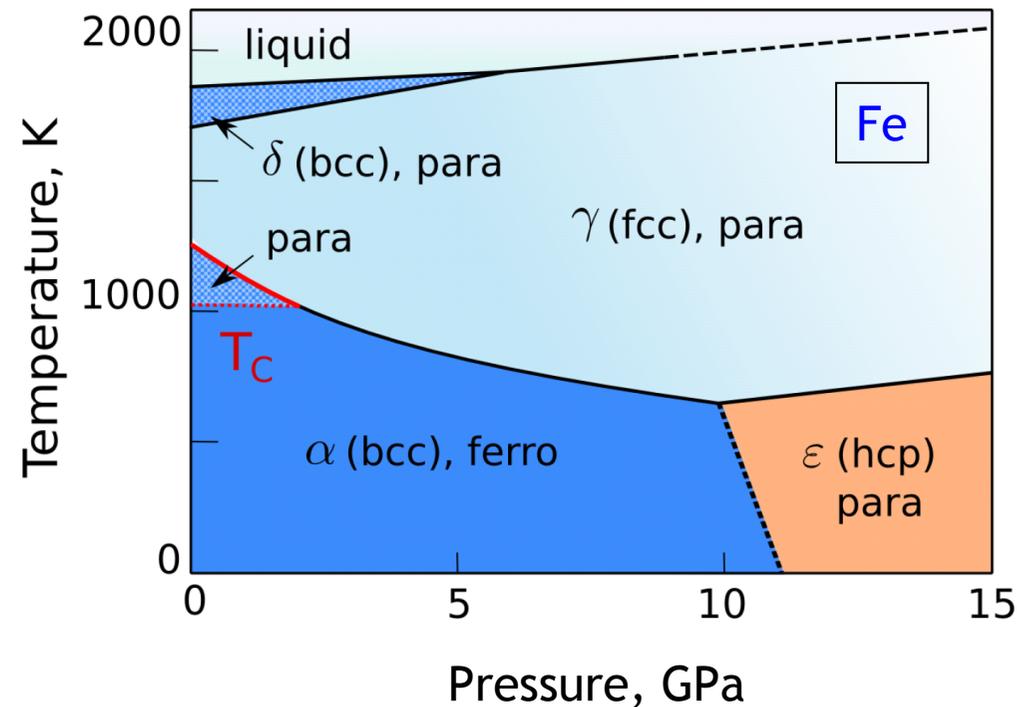
### 3. Correlation-induced lattice transformations

# Application of LDA+DMFT

$\alpha$ - $\gamma$  structural phase transition in paramagnetic Fe

Leonov, Poteryaev, Anisimov, DV; PRL **106**, 106405 (2011)

## Electronic correlations at the $\alpha$ - $\gamma$ structural phase transition in paramagnetic Fe

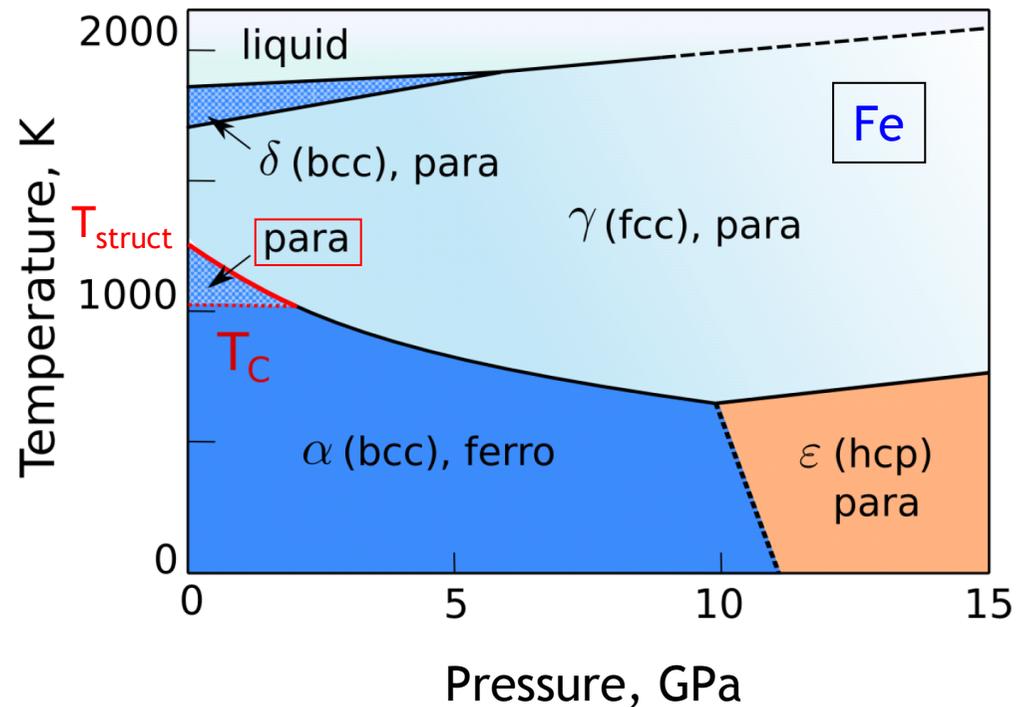


*bcc* structure at  $T \rightarrow 0$ : **exceptional** (covalency, magnetism, ...)

In general:

- Cohesion prefers close packed structure (*fcc*, *hcp*) for  $T \rightarrow 0$
- *bcc* at higher  $T$  (lattice vibrations)

## Electronic correlations at the $\alpha$ - $\gamma$ structural phase transition in paramagnetic Fe



→ Separation of magnetism and structure: Difficult theoretical problem

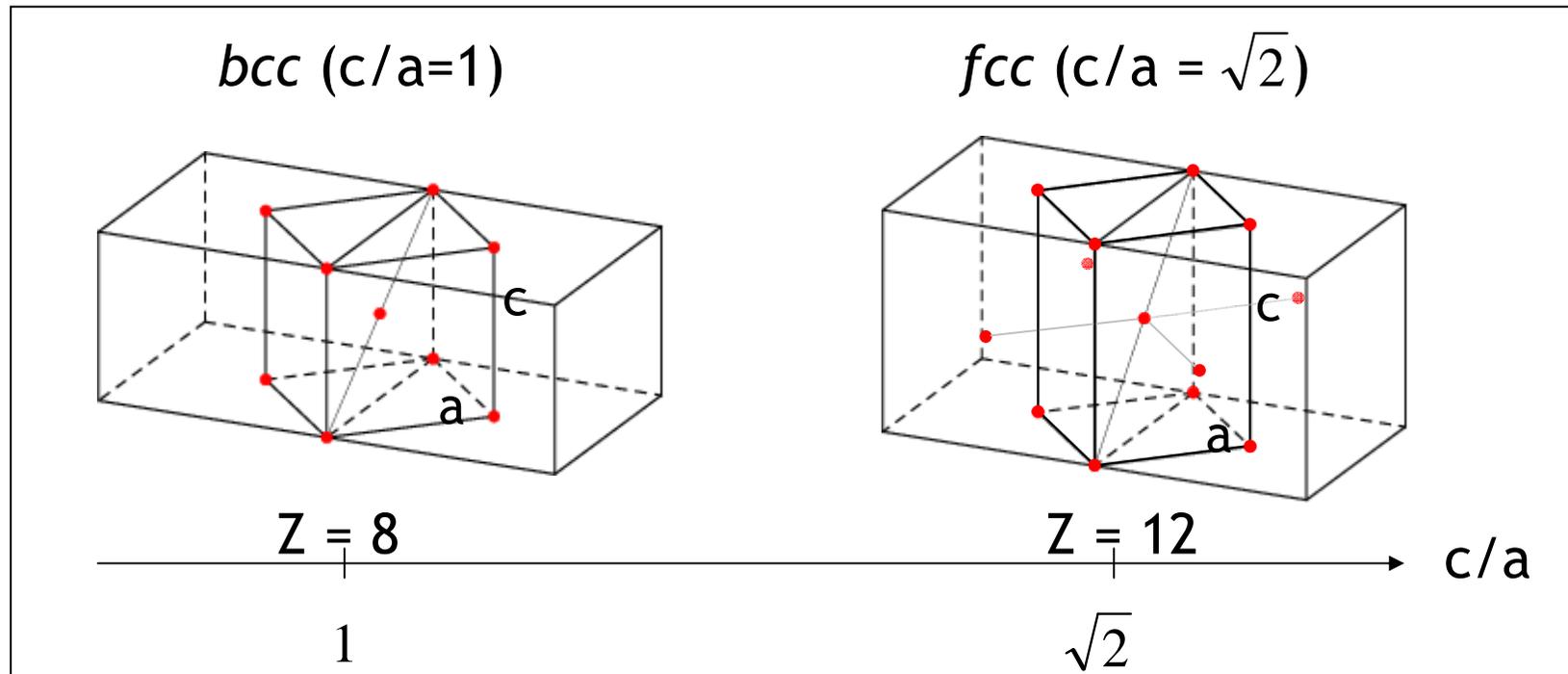
DFT(GGA): finds paramagnetic bcc structure to be unstable

# *bcc-fcc* structural phase transition in paramagnetic Fe

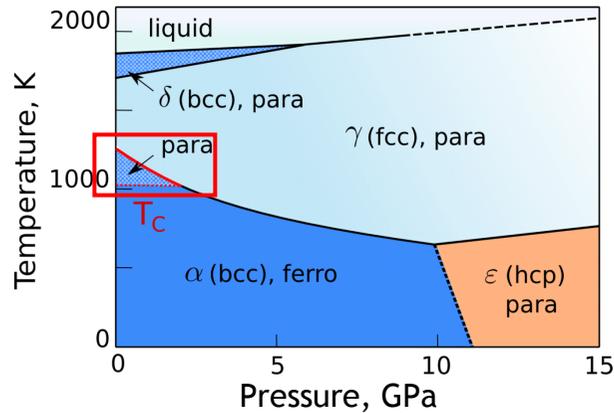
Total energies calculated along *bcc-fcc* Bain transformation path:

Bain and Dunkirk (1924)

Continuous transformation path to account for *bcc-fcc* transition in Fe



# *bcc-fcc* structural phase transition in paramagnetic Fe



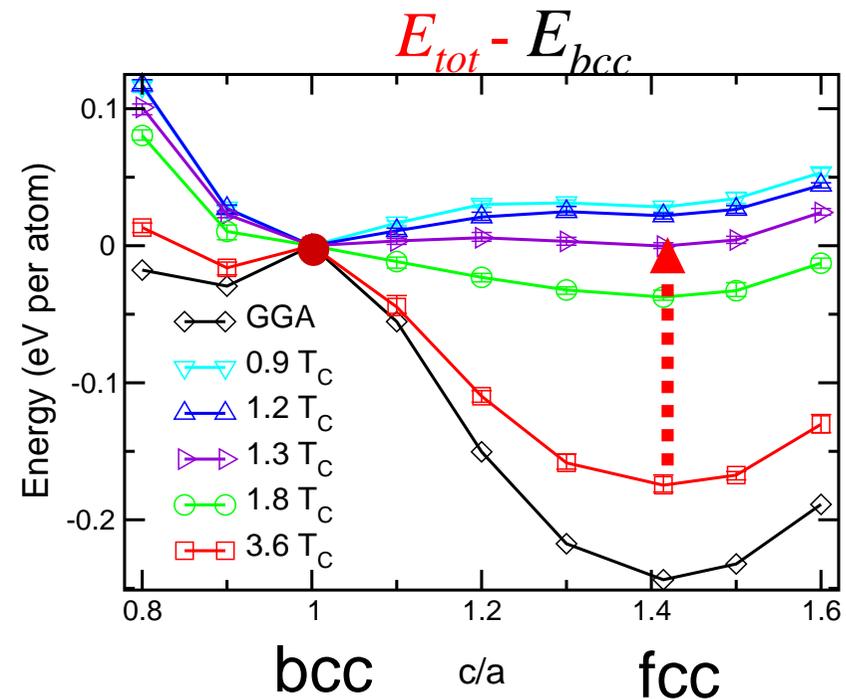
Why is the low-T paramagnetic *bcc* phase stable ?

GGA:  
paramagnetic *fcc* structure stable

GGA+DMFT:

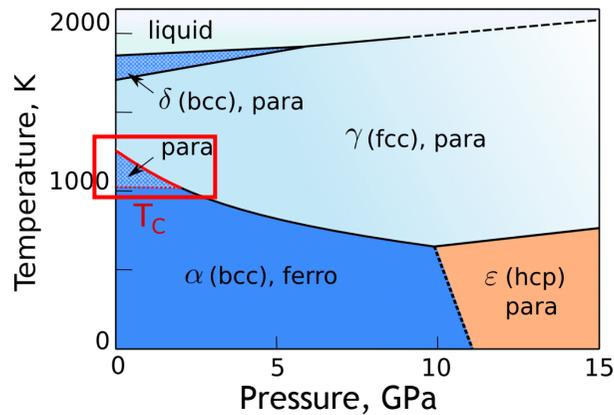
- *bcc-fcc* structural phase transition at  $T_{\text{struct}} \approx 1.2 T_C > T_C$
- LDA+DMFT and GGA+DMFT: qualitatively similar results

GGA+DMFT total energy



What determines the temperature and  $c/a$  dependence of the total energy?

## *bcc-fcc* structural phase transition in paramagnetic Fe



Why is the low-T paramagnetic *bcc* phase stable ?

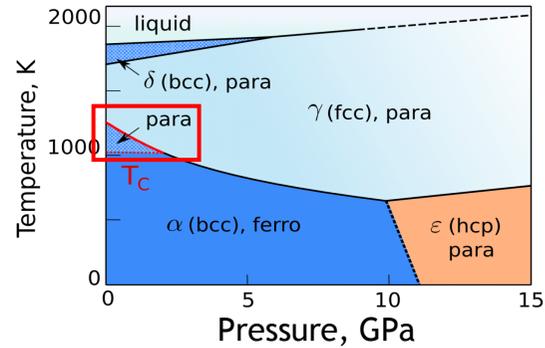
Magnetic correlation energy of the **electrons** ( $\sim -\langle \hat{m}_z^2 \rangle$ ) stabilizes *bcc* **structure**  $\rightarrow T_{\text{struct}} > T_C$

# Application of LDA+DMFT

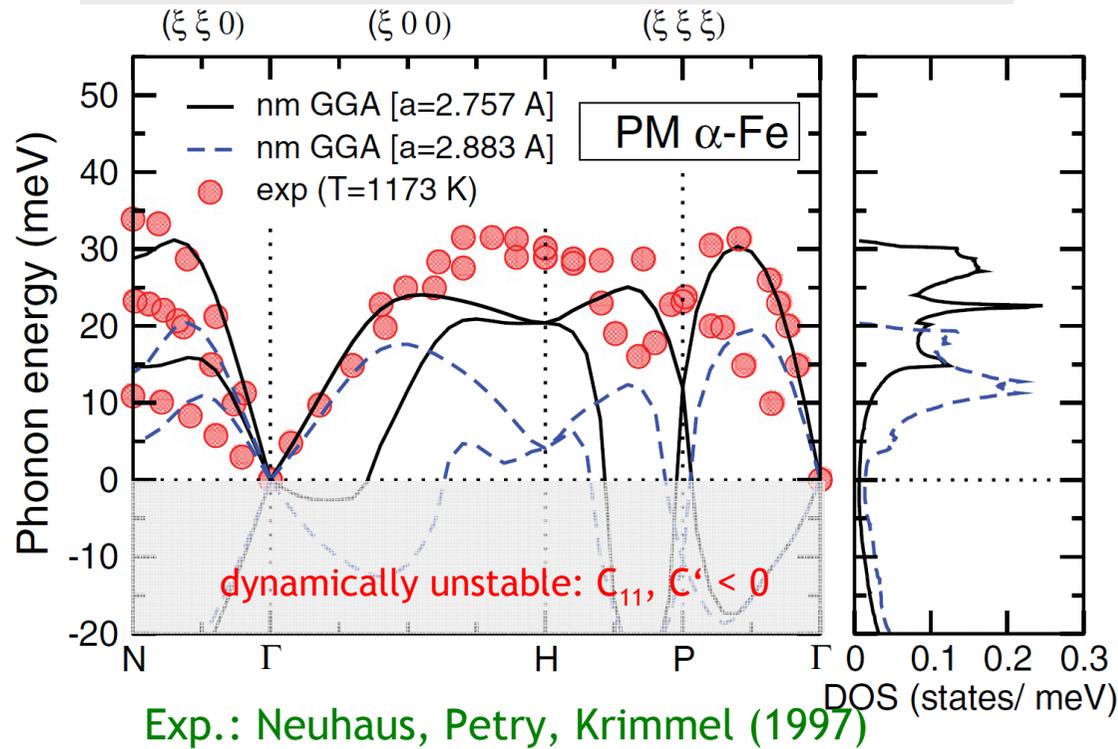
Lattice dynamics and phonon spectra of Fe

Leonov, Poteryaev, Anisimov, DV; PRB **85**, 020401(R) (2012)

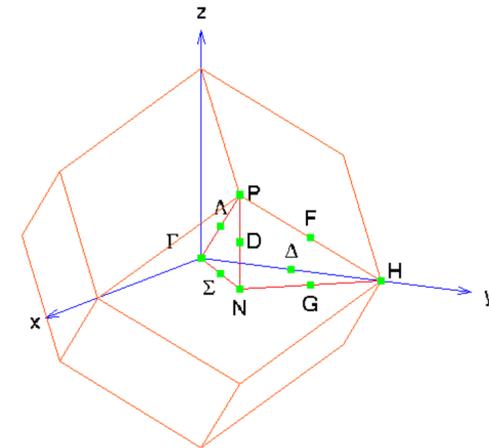
# Lattice dynamics of paramagnetic *bcc* iron



## Non-magnetic GGA phonon dispersion



## 1. Brillouin zone



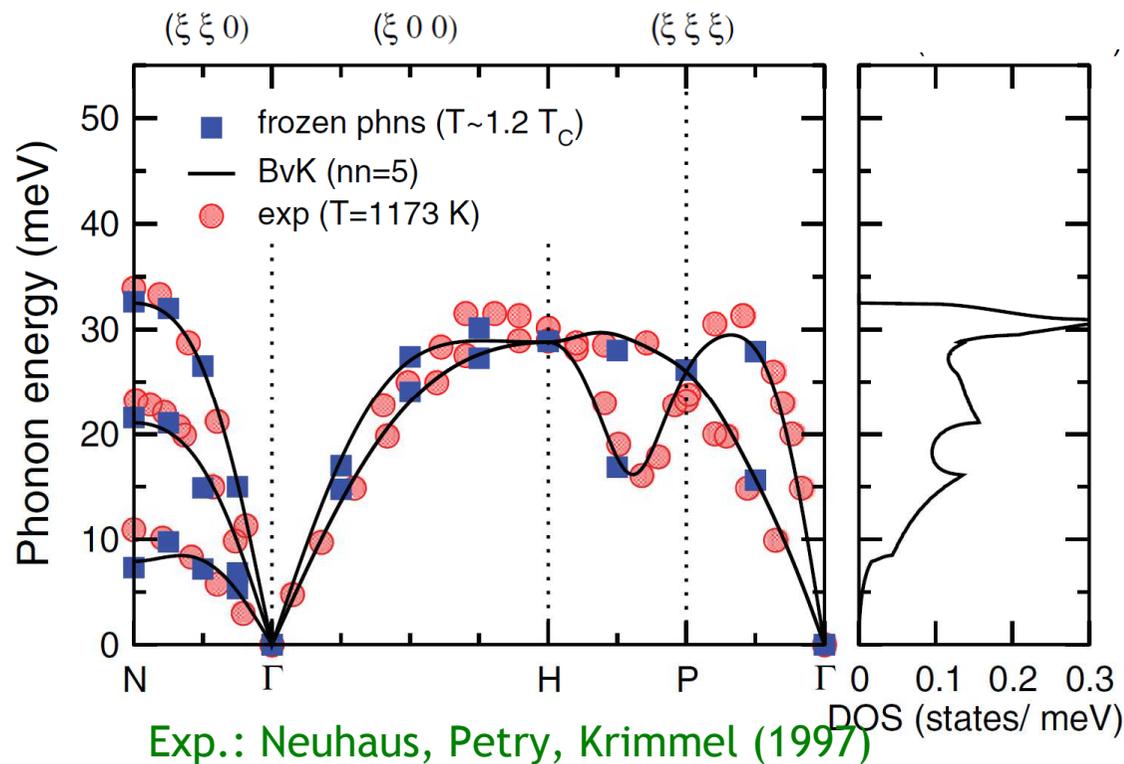
Leonov, Poteryaev, Anisimov, DV (2012)



# Lattice dynamics of paramagnetic *bcc* iron

- phonon frequencies calculated with frozen-phonon method
  - harmonic approximation
- Stokes, Hatch, Campbell (2007)

## GGA+DMFT phonon dispersion at $1.2 T_C$



Electronic correlations  
strongly influence  
lattice-dynamical  
properties

Leonov, Poteryaev,  
Anisimov, DV (2012)



Herzlichen Glückwunsch, Gernot!